Algebra IA:	MODULE 1/UNIT 1:	Operations and Linear Equations & Inequalities:	TIME FRAME:	Ongoing
Gr. 9		Operations with Real Numbers and Expressions		0 0

NATIONAL COMMON CORE STANDARDS:

Use properties of rational and irrational numbers.

• **N.RN.3** Explain why the sum or product of two rational numbers is rational; that the sum of a rational number and an irrational number is irrational; and that the product of a nonzero rational number and an irrational number is irrational.

Interpret the structure of expressions.

- A.SSE.1 Interpret expressions that represent a quantity in terms of its context.
 - a. Interpret parts of an expression, such as terms, factors, and coefficients.

Understand solving equations as a process of reasoning and explain the reasoning.

• A.REI.1 Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

MATHEMATICAL PRACTICES:

- 1. Make sense of problems and persevere in solving them.
- **2.** Reason abstractly and quantitatively.
- **3.** Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- 6. Attend to precision.
- **7.** Look for and make use of structure.
- **8.** Look for and express regularity in repeated reasoning.

ESSENTIAL QUESTIONS	VOCABULARY		ASSESSMENT	
 How do you compare and/or order real numbers? How are radical expressions represented? What are the characteristics of square root functions? How can you represent very large and very small numbers? How can you simplify expressions involving exponents and/or absolute value? Can two algebraic expressions that appear to be different be equivalent? 	real numbers natural numbers whole numbers integers rational numbers irrational numbers simplify evaluate distributive property like terms	absolute value inverse operations equation inequality domain function percent of change ratio proportion square root	Formative: Journals/logs KWL chart At the bell activities Question and answer Individual white boards/Promethean Board ActiVotes Homework Quizzes Constructed response/openended problem solving Performance tasks Exit slips	
			Summative:	

	PA COMMON CORE STANDARDS	KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES
	CC.2.1.6.E.3: Develop and/or apply number theory concepts to find common factors and multiples.	A1.1.1 Operations with Real Numbers and Expressions
	CC.2.2.7.B.3: Model and solve real-world and mathematical problems by using and connecting numerical, algebraic, and/or graphical representations. CC.2.1.8.E.1: Distinguish between rational and irrational numbers using their properties. CC.2.1.8.E.4: Estimate irrational numbers by comparing them to rational numbers. CC.2.1.HS.F.2: Apply properties of rational and irrational numbers to solve real-world or	A1.1.1.1 Represent and/or use numbers in equivalent forms (e.g., integers, fractions, decimals, percents, square roots, and exponents).
PRESSIONS	mathematical problems. CC.2.2.HS.D.1: Interpret the structure of expressions to represent a quantity in terms of its context. CC.2.2.HS.D.2 Write expressions in equivalent forms to solve problems. CC.2.2.HS.D.6	 A1.1.1.1 Compare and/or order any real numbers. Note: Rational and irrational may be mixed.
TION: RS AND EXI	Extend the knowledge of rational functions to rewrite in equivalent forms. CC.2.2.HS.D.9 Use reasoning to solve equations and justify the solution method.	A1.1.1.2 Apply number theory concepts to show relationships between real numbers in problem solving settings.
UNIT OF INSTRUCTION: OPERATIONS WITH REAL NUMBERS AND EXPRESSIONS	 Essential Skills and Understanding Ability to perform operations on both rational and irrational numbers. Ability to make connections between symbolic representations and proper mathematics vocabulary for linear expressions. Ability to identify parts of an expression such as terms, factors, coefficients, etc. for linear expressions. Ability to interpret and apply rules for order of operations for linear expressions. Ability to use properties of mathematics to alter the structure of an expression. Ability to identify the mathematic property (addition property of equality, distributive property, etc.) used at each step in the solution process as a means of justifying a step. 	 A1.1.1.3 Use exponents, roots, and/or absolute values to solve problems. A1.1.1.3.1 Simplify/evaluate expressions involving properties/laws of exponents, roots, and/or absolute values to solve problems. Note: Exponents should be integers from -10 to 10. A1.1.1.4 Use estimation strategies in problem-solving situations. A1.1.1.4.1 Use estimation to solve problems.

	DIFFERENTIATION AC Teacher directed differentiated instructional projects and ac		
ENRICHMENT:	Pearson SuccessNet On-Line Teacher's Edition Pearson on-line resources and materials Studylsland Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks http://www.artofproblemsolving.com/liz/Alcumus/index.php Enrichment based on student GIEP or need of student	REMEDIATION:	Pearson Successnet On-Line Teacher's Edition Pearson on-line resources and materials Web-based Math Resources Supporting the range of learners as per teacher manual Teacher generated/differentiated instruction activities Small group instruction Adapted assignments Additional time Alternative Assessments Chunking of content, assignment and/or assessments One-on-one re-teaching Volunteer/peer tutoring Accommodations based on IEP and/or need ELL student(or based on student need) additional support Provide specific examples Use of Manipulatives Simplified language in word problems Visuals Flashcards Multiple-meaning words Bilingual dictionary/picture dictionary Math Support, Learning Support, or ELL Teachers as appropriate and based on need

RESOURCES:

- Pearson Algebra I: Units 1, 2, 3, 4
- PDE SAS portal: http://www.pdesas.org
- Thinking Maps
- Graphing calculator
- Exit Tickets
- Adaptions checklist
- ELL Instructional Strategies for Math
- ESL Handbook
 - o Click on "Academic Resources" from PMSD website
 - Click on "ESL" on left side of tool bar.
 - o Click on the link to the PMSD ESEL Handbook
 - Scroll through to page 44 in the appendices.
- Teacher generated/differentiated instruction resources and activities
- Algebra I released state sample questions
- Algebra I generated sample guestions
- Promethean Flipcharts/ActiveVotes
- Math flipcharts
- Math Internet Resources from PMSD Resource Page
- StudyIsland
- http://www.khanacademy.org/
- Thinkfinity website: http://www.thinkfinity.org/home
- IXL Website: http://www.IXL.com/math/
- United Streaming: http://streaming.discoveryeducation.com/index.cfm
- http://edhelper.com/place value.html
- http://illuminations.nctm.org
- http://insidemathematics.org
- www.teachingchannel.org
- www.Learnzillion.com
- http://illustrativemathematics.org/standards/k8
- http://wiki.warren.kyschools.us/groups/wcpscommoncorestandards/
- www.teachingchannel.org
- http://www.learnzillion.com
- http://www.teacherspayteachers.com
- flexmath.ck12.org/

Algebra IA: Gr. 9	MODULE 1/UNIT 2:	Operations and Linear Equations & Inequalities: Linear Equations	TIME FRAME:	Ongoing
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NATIONAL COMMON CORE STANDARDS:

Reason quantitatively and use units to solve problems.

- **N.Q.1** Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.
- N.Q.2 Define appropriate quantities for the purpose of descriptive modeling.
- N.Q.3 Choose a level of accuracy appropriate to limitations on measurement when reporting quantities.

Understand the concept of a function and use function notation.

- **F.IF.1** Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input x. The graph of f is the graph of the equation y = f(x).
- **F.IF.2** Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.
- **F.IF.3** Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. For example, the Fibonacci sequence is defined recursively by f(0) = f(1) = 1, f(n+1) = f(n) + f(n-1) for $n \ge 1$.

Interpret functions that arise in applications in terms of a context.

- **F.IF.4** For a function that models a relationship between two quantities, interpret key features of the graph and the table in terms of the quantities, and sketch the graph showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.
- **F.IF.5** Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function h(n) gives the number of person-hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.
- **F.IF.7** Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
 - a. Graph **linear** and quadratic functions and show **intercepts**, maxima, and minima.

Build a function that models a relationship between two quantities.

- F.BF.1 Write a function that describes a relationship between two quantities.
 - a. Determine an explicit expression, a recursive process, or steps for calculations from a context.
- **F.BF.2** Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms.

MATHEMATICAL PRACTICES:

- 1. Make sense of problems and persevere in solving them.
- **2.** Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- Model with mathematics.
- **5.** Use appropriate tools strategically.
- 6. Attend to precision.
- **7.** Look for and make use of structure.
- **8.** Look for and express regularity in repeated reasoning.

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Create equations that describe numbers or relationships.

- **A.CED.1** Create equations and inequalities in one variable and use them to solve problems. *Include* equations arising from linear and quadratic functions, and simple rational and exponential functions.
- **A.CED.2** Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
- **A.CED.3** Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or non-viable options in a modeling context. For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.
- **A.CED.4** Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law V = IR to highlight resistance R.

Represent and solve equations and inequalities graphically.

• **A.REI.11** Explain why the x-coordinates of the points where the graphs of the equations y = f(x) and y = g(x) intersect are the solutions of the equation f(x) = g(x); find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where f(x) and/or g(x) are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.

UNIT OF INSTRUCTION: LINEAR EQUATIONS

POCONO MOUNTIAN SCHOOL DISTRICT CURRICULUM

PA COMMON CORE STANDARDS **KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES** CC.2.2.8.B.3: Analyze and solve linear equations and pairs of simultaneous linear A1.1.2 Linear Equations eauations. CC.2.2.8.C.1: Define, evaluate, and compare functions. A1.1.2.1 Write, solve, and/or graph linear equations CC.2.2.8.C.2: Use concepts of functions to model relationships between using various methods. auantities. CC.2.1.HS.F.3: Apply quantitative reasoning to choose and interpret units and A1.1.2.1.1 scales in formulas, graphs, and data displays. • Write, solve, and/or apply linear equation CC.2.1.HS.F.4: Use units as a way to understand problems and to guide the (including problem situations). solution of multi-step problems. A1.1.2.1.2 **CC.2.1.HS.F.5:** Choose a level of accuracy appropriate to limitations on Use and/or identify an algebraic property to justify any step in an equation-solving process. measurement when reporting quantities. CC.2.2.HS.C.3: Write functions or sequences that model relationships between Note: Linear equations only. two quantities. A1.1.2.1.3 CC.2.2.HS.D.7: • Interpret solutions to problems in the context of the problem situation. Note: Linear equations Create and graph equations or inequalities to describe numbers or relationships. only. CC.2.2.HS.D.8: Apply inverse operations to solve equations or formulas for a A1.1.2.2 Write, solve, and/or graph systems of linear given variable. equations using various methods. CC.2.2.HS.D.9: Use reasoning to solve equations and justify the solution method. CC.2.2.HS.D.10: Represent, solve, and interpret equations/inequalities and A1.1.2.2.1 systems of equations/inequalities algebraically and graphically. • Write and/or solve a system of linear equations (including problem situations) using graphing, **Essential Skills and Understanding** substitution, and/or elimination. Note: Limit Ability to choose appropriate units of measure to represent context of systems to two linear equations. the problem. A1.1.2.2.2 Ability to convert units of measure using dimensional analysis. Ability to select and use units of measure to accurately model a given Interpret solutions to problems in the context of the problem situation. Note: Limit systems to real world scenario. two linear equations. Knowledge of and ability to apply rules of significant digits. Ability to use precision of initial measurements to determine the level of precision with which answers can be reported. Ability to solve linear equations. Ability to set up and solve proportions. Ability to determine if a relation is a function. Ability to identify the domain and range of a function from multiple representations. Ability to use functional notation.

Knowledge of and ability to apply the vertical line test.

of linear functions.

Ability to write arithmetic sequences and the relationship as an example

	PA COMMON CORE STANDARDS	KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES
UNIT OF INSTRUCTION: LINEAR EQUATIONS	 Ability to relate the concept of domain to each function studied. Ability to translate from algebraic representations to graphic or numeric representations and identify key features using the various representations. Ability to describe the restrictions on the domain of all functions based on real world context. Ability to graph linear functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. Ability to write a function that describes a relationship between two quantities. Ability to create equations in one variable and use them to solve problems. Ability to find solutions of systems of linear equations in real world situations. Ability to determine unknown parameters needed to create an equation that accurately models a given situation. Ability to represent constraints by equations and by systems of equations and interpret solutions as viable or non-viable options in a modeling context. Ability to distinguish between a mathematical solution and a contextual solution. Ability to recognize/create equivalent forms of literal equations. 	

DIFFERENTIATION ACTIVITIES: Teacher directed differentiated instructional projects and activities are ongoing and based on student need. Pearson SuccessNet On-Line Teacher's Edition Pearson on-line resources and materials StudyIsland Pearson on-line resources and materials Web-based Math Resources					
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 Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks http://www.artofproblemsolving.com/liz/Alcumus/index.php Enrichment based on student GIEP or need of student Supporting the range of learners as per teacher manual Teacher generated/differentiated instruction activities Small group instruction Adapted assignments Additional time Alternative Assessments Chunking of content, assignment and/or assessments 	ction				

ENRICHMENT

REMEDIATION

- ELL student(or based on student need) additional support
 - o <u>Provide specific examples</u>
 - o <u>Use of Manipulatives</u>
 - o Simplified language in word problems

Accommodations based on IEP and/or need

- o <u>Visuals</u>
- o <u>Flashcards</u>

One-on-one re-teaching Volunteer/peer tutoring

- o <u>Multiple-meaning words</u>
- o <u>Bilingual dictionary/picture dictionary</u>
- Math Support, Learning Support, or ELL Teachers as appropriate and based on need

RESOURCES

- Pearson Algebra I: Units 3, 5, 7
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- ESL Handbook
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 - Click on "ESL" on left side of tool bar.
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- StudyIsland
- http://www.khanacademy.org/
- Thinkfinity website: http://www.thinkfinity.org/home
- IXL Website: http://www.IXL.com/math/
- United Streaming: http://streaming.discoveryeducation.com/index.cfm
- http://edhelper.com/place_value.html
- http://illuminations.nctm.org
- http://insidemathematics.org
- www.teachingchannel.org
- www.Learnzillion.com
- http://illustrativemathematics.org/standards/k8
- http://wiki.warren.kyschools.us/groups/wcpscommoncorestandards/
- www.teachingchannel.org
- http://www.learnzillion.com
- http://www.teacherspayteachers.com
- flexmath.ck12.org/

Algebra IA: Gr. 9 MODULE 1/UNIT 3: Operations and Linear Equations & Inequalities: Linear Inequalities TIME FRAME	Ongoing
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NATIONAL COMMON CORE STANDARDS:

Reason quantitatively and use units to solve problems.

- **N.Q.1** Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.
- N.Q.2 Define appropriate quantities for the purpose of descriptive modeling.
- **N.Q.3** Choose a level of accuracy appropriate to limitations on measurement when reporting quantities.

Interpret functions that arise in applications in terms of a context.

- **F.IF.4** For a function that models a relationship between two quantities, interpret key features of the graph and the table in terms of the quantities, and sketch the graph showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.
- **F.IF.5** Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function h(n) gives the number of person-hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.
- **F.IF.7** Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
 - a. Graph **linear** and quadratic functions and show **intercepts**, maxima, and minima.

Create equations that describe numbers or relationships.

- **A.CED.1** Create equations and inequalities in one variable and use them to solve problems. *Include* equations arising from linear and quadratic functions, and simple rational and exponential functions.
- **A.CED.2** Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
- **A.CED.3** Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or non-viable options in a modeling context. For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.

Represent and solve equations and inequalities graphically.

• **A.REI.11** Explain why the x-coordinates of the points where the graphs of the equations y = f(x) and y = g(x) intersect are the solutions of the equation f(x) = g(x); find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where f(x) and/or g(x) are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.

MATHEMATICAL PRACTICES:

- 1. Make sense of problems and persevere in solving them.
- **2.** Reason abstractly and quantitatively.
- 3. Construct viable arguments and critique the reasoning of others.
- **4.** Model with mathematics.
- **5.** Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- **8.** Look for and express regularity in repeated reasoning.

	PA COMMON CORE STANDARDS	KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES
	CC.2.1.HS.F.5: Choose a level of accuracy appropriate to limitations on	A1.1.3 Linear Inequalities
	measurement when reporting quantities.	
	CC.2.2.HS.D.7:	A1.1.3.1 Write, solve, and/or graph linear inequalities
ES S	Create and graph equations or inequalities to describe numbers or relationships.	using various methods.
일 별	CC.2.2.HS.D.9: Use reasoning to solve equations and justify the solution method.	
ICI AL	CC.2.2.HS.D.10: Represent, solve, and interpret equations/inequalities and	A1.1.3.1.1
INSTRUCTION INEQUALITIES	systems of equations/inequalities algebraically and graphically.	Write or solve compound inequalities and/or
NS NE	- "	graph their solution sets on a number line (may
╙ ~	Essential Skills and Understanding	include absolute value inequalities).
O E	 Ability to choose appropriate units of measure to represent context of 	A1.1.3.1.2
UNIT O	the problem.	Identify or graph the solution set to a linear
D -	 Ability to convert units of measure using dimensional analysis. 	inequality on a number line.
	 Ability to select and use units of measure to accurately model a given 	A1.1.3.1.3
	real world scenario.	Interpret solutions to problems in the context of
	 Knowledge of and ability to apply rules of significant digits. 	the problem situation. Note: Linear inequalities
		only.

PA COMMON CORE STANDARDS **KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES** A1.1.3.2 Write, solve, and/or graph systems of linear Ability to use precision of initial measurements to determine the level of inequalities using various methods. precision with which answers can be reported. Ability to identify the domain and range of a function from multiple representations. A1.1.3.2.1 Ability to relate the concept of domain to each function studied. • Write and/or solve a system of linear Ability to translate from algebraic representations to graphic or numeric inequalities using graphing. Note: Limit systems representations and identify key features using the various to two linear inequalities. representations. A1.1.3.2.2 Ability to describe the restrictions on the domain of all functions based • Interpret solutions to problems in the context of the problem situation. Note: Limit systems to on real world context. Ability to graph linear inequalities expressed symbolically and show key two linear inequalities. features of the graph, by hand in simple cases and using technology for more complicated cases. Ability to write inequalities that describes a relationship between two auantities. Ability to create inequalities in one variable and use them to solve problems. Ability to find solutions of systems of linear inequalities in real world situations. Ability to determine unknown parameters needed to create an inequality that accurately models a given situation. Ability to represent constraints by inequalities and by systems of inequalities and interpret solutions as viable or non-viable options in a modeling context. Ability to distinguish between a mathematical solution and a contextual solution. Ability to solve absolute value equations and inequalities.

Teach	DIFFERENTIATION ACTIV ner directed differentiated instructional projects and activities are ongoing of		
<u>ENRICHMENT:</u>	 Pearson SuccessNet On-Line Teacher's Edition Pearson on-line resources and materials StudyIsland Web-based Math Resources Small group instruction Teacher generated/differentiated instruction enrichment and activities Supporting the range of learners as per teacher manual Encourage and support learners in explaining how they applied their skills during mathematical tasks http://www.artofproblemsolving.com/liz/Alcumus/index.php Enrichment based on student GIEP or need of student 	REMEDIATION:	 Pearson Successnet On-Line Teacher's Edition Pearson on-line resources and materials Web-based Math Resources Supporting the range of learners as per teacher manual Teacher generated/differentiated instruction activities Small group instruction Adapted assignments Additional time Alternative Assessments Chunking of content, assignment and/or assessments One-on-one re-teaching Volunteer/peer tutoring Accommodations based on IEP and/or need ELL student (or based on student need) additional support Provide specific examples Use of Manipulatives Simplified language in word problems Visuals Flashcards Multiple-meaning words Bilingual dictionary/picture dictionary Math Support, Learning Support, or ELL Teachers as appropriate and based on need

RESOURCES

- Pearson Algebra I: Unit 4, 7
- PDE SAS portal: http://www.pdesas.org
- Thinking Maps
- Graphing calculator
- Exit Tickets
- Adaptions checklist
- ELL Instructional Strategies for Math
- ESL Handbook
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- IXL Website: http://www.IXL.com/math/
- United Streaming: http://streaming.discoveryeducation.com/index.cfm
- http://edhelper.com/place_value.html
- http://illuminations.nctm.org
- http://insidemathematics.org
- www.teachingchannel.org
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- http://www.learnzillion.com
- http://www.teacherspayteachers.com
- flexmath.ck12.org/

Algebra IA: Gr. 9 MODULE 2/UNIT 4: Linear Functions and Data Organizations: Functions TIME FRAME: O	Ongoing
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NATIONAL COMMON CORE STANDARDS:

Understand the concept of a function and use function notation.

- **F.IF.1** Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input x. The graph of f is the graph of the equation y = f(x).
- **F.IF.2** Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.
- **F.IF.3** Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers. For example, the Fibonacci sequence is defined recursively by f(0) = f(1) = 1, f(n+1) = f(n) + f(n-1) for n ≥ 1. Learn as general principle; focus on linear and exponential and on arithmetic and geometric sequences.

Interpret functions that arise in applications in terms of a context.

- **F.IF.4** For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.
- **F.IF.5** Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function h(n) gives the number of person hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.
- **F.IF.6** Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.

Analyze functions using different representations.

- **F.IF.7** Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
 - a. Graph linear and quadratic functions and show intercepts, maxima, and minima.

Build a function that models a relationship between two quantities.

- **F.BF.1** Write a function that describes a relationship between two quantities.

 a. Determine an explicit expression, a recursive process, or steps for calculations from a context.
- **F.BF.2** Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms.

Build new functions from existing functions.

• **F.BF.3** Identify the effect on the graph of replacing f(x) by f(x) + k, k f(x), f(kx), and f(x + k) for specific values of k (both positive and negative); find the value of k given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and

MATHEMATICAL PRACTICES:

- 1. Make sense of problems and persevere in solving them.
- **2.** Reason abstractly and quantitatively.
- **3.** Construct viable arguments and critique the reasoning of others.
- **4.** Model with mathematics.
- **5.** Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- **8.** Look for and express regularity in repeated reasoning.

odd functions from their graphs and algebraic expressions for them.

Construct and compare linear, quadratic, and exponential models and solve problems.

- **F.LE.2** Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table).
- **F.LE.3** Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function.

Summarize, represent, and interpret data on two categorical and quantitative variables.

- **S.ID.5** Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data.
- **S.ID.6** Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.
 - a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.

c. Fit a linear function for a scatter plot that suggests a linear association.

c. Fit a linear function for a scatter plot that sug	ggests a linear association.	
ESSENTIAL QUESTIONS	VOCABULARY	ASSESSMENT
	VOCABULARY linear equation arithmetic sequence common difference term continuous data discrete data relation function function notation vertical line test domain range translation	Formative: Journals/logs KWL chart At the bell activities Question and answer Individual white boards/Promethean Board Activotes Homework Quizzes Constructed response/openended problem solving Performance tasks
	linear function graph absolute value function graph	 Exit slips Summative: CDT's Performance based assessments Quizzes Tests Constructed response/openended problem solving Performance tasks Project

UNIT OF INSTRUCTION:

	PA COMMON CORE STANDARDS	KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES
UNIT OF INSTRUCTION: FUNCTIONS	CC.2.2.8.B.2: Understand the connections between proportional relationships, lines, and linear equations. CC.2.2.8.C.1: Define, evaluate, and compare functions. CC.2.2.8.C.2: Use concepts of functions to model relationships between quantities. CC.2.2.HS.C.1: Use the concept and notation of functions to interpret and apply them in terms of their context. CC.2.2.HS.C.2: Graph and analyze functions and use their properties to make connections between the different representations. CC.2.2.HS.C.3: Write functions or sequences that model relationships between two quantities. CC.2.2.HS.C.4: Interpret the effects transformations have on functions and find the inverses of functions. CC.2.2.HS.C.6: Interpret functions in terms of the situations they model. CC.2.4.HS.B.2: Summarize, represent, and interpret data on two categorical and quantitative variables. CC.2.1.HS.F.3: Apply quantitative reasoning to choose and interpret units and scales in formulas, graphs, and data displays. CC.2.1.HS.F.4: Use units as a way to understand problems and to guide the solution of multi-step problems.	 A1.2.1 Functions A1.2.1.1 Analyze and/or use patterns or relations. A1.2.1.1.1 Analyze a set of data for the existence of a pattern and represent the pattern algebraically and/or graphically. A1.2.1.1.2 Determine whether a relation is a function, given a set of points or a graph. A1.2.1.1.3 Identify the domain or range of a relation (may be presented as ordered pairs, a graph, or a table).
FUN	 Essential Skills and Understanding Ability to determine if a relation is a function. Ability to analyze data for the existence of a pattern and represent the pattern algebraically and/or graphically. Ability to determine whether a relation is a function, given a set of points or a graph. Ability to identify the domain and range of a function from multiple representations. Ability to use of function notation. Knowledge of and ability to apply the vertical line test. Ability to make connections between context and algebraic representations which use function notation to write arithmetic sequences. Emphasize arithmetic sequences as examples of linear functions. Ability to translate from algebraic representations to graphic or numeric representations and identify key features using the various representations. Ability to relate the concept of domain to each function studied. Ability to describe the restrictions on the domain of all functions based on real world context. Knowledge that the rate of change of a function can be positive, negative, zero, or none. Ability to identify the rate of change from multiple representations. Determine an explicit expression, a recursive process, or steps for calculations from a 	 A1.2.1.2 Interpret and/or use linear functions and their equations, graphs, or tables. A1.2.1.2.1 Create, interpret, and/or use the equation, graph, or table of a linear function. A1.2.1.2.2 Translate from one representation of a linear function to another (i.e., graph, table, and equation).

PA COMMON CORE STANDARDS	KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES
 context. Ability to focus on vertical translations of graphs of linear functions. Relate the vertical translation of a linear function to its y-intercept. Ability to compare the graphs of linear functions and absolute value functions and identify main components and equations for each. Knowledge of the characteristics of categorical data. Ability to recognize types of relationships that lend themselves to linear and exponential models. Ability to create and use regression models to represent a contextual situation. 	

DIFFERENTIATION ACTIVITIES:

REMEDIATION:

Teacher directed differentiated instructional projects and activities are ongoing and based on student need.

 Pearson Succe 	ssNet On-Line	Teacher's	Edition
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- Pearson on-line resources and materials
- StudyIsland
- Web-based Math Resources
- Small group instruction
- Teacher generated/differentiated instruction enrichment and activities
- Supporting the range of learners as per teacher manual
- Encourage and support learners in explaining how they applied their skills during mathematical tasks
- http://www.artofproblemsolving.com/liz/Alcumus/index.php
- Enrichment based on student GIEP or need of student

Pearson Successnet On-Line Teacher's Edition

- Pearson on-line resources and materials
- Web-based Math Resources
- Supporting the range of learners as per teacher manual
- Teacher generated/differentiated instruction activities
- Small group instruction
- Adapted assignments
- Additional time
- Alternative Assessments
- Chunking of content, assignment and/or assessments
- One-on-one re-teaching
- Volunteer/peer tutoring
- Accommodations based on IEP and/or need
- ELL student(or based on student need) additional support
 - Provide specific examples
 - Use of Manipulatives
 - Simplified language in word problems
 - Visuals
 - Flashcards
 - Multiple-meaning words
 - Bilingual dictionary/picture dictionary
- Math Support, Learning Support, or ELL Teachers as appropriate and based on need

ENRICHMENT:

Algebra IA Functions cs 7/2013 4

- Pearson Algebra I: Units 5, 6
- PDE SAS portal: http://www.pdesas.org
- Thinking Maps
- Graphing calculator
- Exit Tickets
- Adaptions checklist
- ELL Instructional Strategies for Math
- ESL Handbook
 - o Click on "Academic Resources" from PMSD website
 - Click on "ESL" on left side of tool bar.
 - Click on the link to the PMSD ESEL Handbook
 - o Scroll through to page 44 in the appendices.
- Teacher generated/differentiated instruction resources and activities
- Algebra I released state sample questions
- Algebra I generated sample questions
- Promethean Flipcharts/ActiveVotes
- Math flipcharts
- Math Internet Resources from PMSD Resource Page
- StudyIsland
- http://www.khanacademy.org/
- Thinkfinity website: http://www.thinkfinity.org/home
- IXL Website: http://www.IXL.com/math/
- United Streaming: http://streaming.discoveryeducation.com/index.cfm
- http://edhelper.com/place_value.html
- http://illuminations.nctm.org
- http://insidemathematics.org
- www.teachingchannel.org
- www.Learnzillion.com
- http://illustrativemathematics.org/standards/k8
- http://wiki.warren.kyschools.us/groups/wcpscommoncorestandards/
- www.teachingchannel.org
- http://www.learnzillion.com
- http://www.teacherspayteachers.com
- <u>flexmath.ck12.org/</u>

RESOURCES

Algebra IA:
Gr. 9

MODULE 2/UNIT 5: Linear Functions and Data Organizations: Coordinate Geometry

TIME FRAME: Ongoing

NATIONAL COMMON CORE STANDARDS:

Understand the concept of a function and use function notation.

- **F.IF.1** Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input x. The graph of f is the graph of the equation y = f(x).
- **F.IF.2** Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

Interpret functions that arise in applications in terms of a context.

- **F.IF.4** For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.
- **F.IF.5** Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function h(n) gives the number of person hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.
- **F.IF.6** Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.

Analyze functions using different representations.

- **F.IF.7** Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
 - a. Graph linear and quadratic functions and show intercepts, maxima, and minima.

Summarize, represent, and interpret data on two categorical and quantitative variables.

- **S.ID.5** Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data.
- **S.ID.6** Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.
 - a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.
 - b. Fit a linear function for a scatter plot that suggests a linear association.

MATHEMATICAL PRACTICES:

- 1. Make sense of problems and persevere in solving them.
- **2.** Reason abstractly and quantitatively.
- **3.** Construct viable arguments and critique the reasoning of others.
- **4.** Model with mathematics.
- **5.** Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- **8.** Look for and express regularity in repeated reasoning.

ESSENTIAL QUESTIONS	VOCABULARY	ASSESSMENT
 What information does the equation of a line give you? How can you make predictions based on a scatter plot? What does the slope of a line indicate about the line? What does the y-intercept indicate about a line? How do you write or identify a linear equation when given the graph of the line, two points on the line, or the slope and a point on the line? How do you represent an equation of a line using a graph, table, and equation? 	linear equation rate of change slope y-intercept x-intercept domain range origin slope-intercept form standard form point-slope form	Formative: Journals/logs KWL chart At the bell activities Question and answer Individual white boards/Promethean Board ActiVotes Homework Quizzes Constructed response/open-ended problem solving Performance tasks Exit slips Summative: CDT's Performance based assessments Quizzes Tests Constructed response/open-ended problem solving Performance based assessments Performance based assessments Project

KEYSTONE ELIGIBLE CONTENT/LEARNING PA COMMON CORE STANDARDS **ACTIVITIES** CC.2.4.8.B.1: Analyze and/or interpret bivariate data displayed in multiple representations. **A1.2.2 Coordinate Geometry** CC.2.2.8.C.2: Use concepts of functions to model relationships between quantities. CC.2.2.HS.C.1: Use the concept and notation of functions to interpret and apply them in A1.2.2.1 Describe, compute, and/or use the terms of their context. rate of change (slope) of a line. CC.2.2.HS.C.2: Graph and analyze functions and use their properties to make connections between the different representations. A1.2.2.1.1 CC.2.2.HS.C.3: Write functions or sequences that model relationships between two • Identify, describe, and/or use constant rates of change. CC.2.2.HS.C.5: Construct and compare linear, quadratic, and exponential models to solve A1.2.2.1.2 • Apply the concept of linear rate of problems. change (slope) to solve problems. **CC.2.2.HS.C.6:** Interpret functions in terms of the situations they model. CC.2.4.HS.B.1: Summarize, represent, and interpret data on a single count or measurement A1.2.2.1.3 • Write or identify a linear equation variable. CC.2.4.HS.B.2: Summarize, represent, and interpret data on two categorical and when given UNIT OF INSTRUCTION: quantitative variables. the graph of the line, CC.2.4.HS.B.3: Analyze linear models to make interpretations based on the data. two points on the line, or o the slope and a point on the **Essential Skills and Understanding** Ability to identify, describe, and/or use constant rates of change. Note: Linear equation may be in Knowledge that the rate of change of a function can be positive, negative, zero, point-slope, standard, and/or slopeintercept form. Ability to identify the rate of change from multiple representations. Ability to identify the domain and range of a function from multiple A1.2.2.1.4 Determine the slope and/or representations. y-intercept represented by a linear Ability to translate from algebraic representations to graphic or numeric equation or graph. representations and identify key features using the various representations. Ability to identify or write a linear equation when given various parts of a linear A1.2.2.2 equation, table or graph. Analyze and/or interpret data on a Ability to determine the slope and/or y-intercept represented by a linear equation scatter plot. or graph. A1.2.2.2.1 Ability to describe the restrictions on the domain of all functions based on real • Draw, identify, find, and/or write an world context. equation for a line of best fit for a Ability to focus on vertical translations of graphs of linear functions. Relate the scatter plot. vertical translation of a linear function to its y-intercept. Knowledge of the characteristics of categorical data. Ability to translate from linear algebraic representations to graphic or numeric representations and identify key features using the various representations. Ability to recognize types of relationships that lend themselves to linear models. Ability to create and use regression models to represent a contextual situation.

	DIFFERENTIATION ACTIVITIES:				
Teac	cher dir	ected differentiated instructional projects and activities are ongoing	g and k	pased o	n student need.
	•	Pearson SuccessNet On-Line Teacher's Edition		•	Pearson Success

- Pearson on-line resources and materials
- StudyIsland
- Web-based Math Resources
- Small group instruction
- Teacher generated/differentiated instruction enrichment and activities
- Supporting the range of learners as per teacher manual
- Encourage and support learners in explaining how they applied their skills during mathematical tasks
- http://www.artofproblemsolving.com/liz/Alcumus/index.php
- Enrichment based on student GIEP or need of student

Pearson Successnet On-Line Teacher's Edition

- Pearson on-line resources and materials
- Web-based Math Resources
- Supporting the range of learners as per teacher manual
- Teacher generated/differentiated instruction activities
- Small group instruction
- Adapted assignments
- Additional time
- Alternative Assessments
- Chunking of content, assignment and/or assessments
- One-on-one re-teaching
- Volunteer/peer tutoring
- Accommodations based on IEP and/or need
- ELL student (or based on student need) additional support
 - o Provide specific examples
 - Use of Manipulatives
 - o Simplified language in word problems
 - Visuals
 - Flashcards
 - Multiple-meaning words
 - Bilingual dictionary/picture dictionary
- Math Support, Learning Support, or ELL Teachers as appropriate and based on need

REMEDIATION:

ENRICHMENT:

RESOURCES:

- Pearson Algebra I: Units 5, 6
- PDE SAS portal: http://www.pdesas.org
- Thinking Maps
- Graphing calculator
- Exit Tickets
- Adaptions checklist
- ELL Instructional Strategies for Math
- ESL Handbook
 - o Click on "Academic Resources" from PMSD website
 - Click on "ESL" on left side of tool bar.
 - o Click on the link to the PMSD ESEL Handbook
 - Scroll through to page 44 in the appendices.
- Teacher generated/differentiated instruction resources and activities
- Algebra I released state sample questions
- Algebra I generated sample questions
- Promethean Flipcharts/ActiveVotes
- Math flipcharts
- Math Internet Resources from PMSD Resource Page
- StudyIsland
- http://www.khanacademy.org/
- Thinkfinity website: http://www.thinkfinity.org/home
- IXL Website: http://www.IXL.com/math/
- United Streaming: http://streaming.discoveryeducation.com/index.cfm
- http://edhelper.com/place value.html
- http://illuminations.nctm.org
- http://insidemathematics.org
- www.teachingchannel.org
- www.Learnzillion.com
- http://illustrativemathematics.org/standards/k8
- http://wiki.warren.kyschools.us/groups/wcpscommoncorestandards/
- www.teachingchannel.org
- http://www.learnzillion.com
- http://www.teacherspayteachers.com
- flexmath.ck12.org/

Algebra IA:
Gr. 9

MODULE 2/UNIT 5: Linear Functions and Data Organizations: Coordinate Geometry

TIME FRAME: Ongoing

NATIONAL COMMON CORE STANDARDS:

Understand the concept of a function and use function notation.

- **F.IF.1** Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input x. The graph of f is the graph of the equation y = f(x).
- **F.IF.2** Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.

Interpret functions that arise in applications in terms of a context.

- **F.IF.4** For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.
- **F.IF.5** Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function h(n) gives the number of person hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.
- **F.IF.6** Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.

Analyze functions using different representations.

- **F.IF.7** Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
 - a. Graph linear and quadratic functions and show intercepts, maxima, and minima.

Summarize, represent, and interpret data on two categorical and quantitative variables.

- **S.ID.5** Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data.
- **S.ID.6** Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.
 - a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.
 - b. Fit a linear function for a scatter plot that suggests a linear association.

MATHEMATICAL PRACTICES:

- 1. Make sense of problems and persevere in solving them.
- **2.** Reason abstractly and quantitatively.
- **3.** Construct viable arguments and critique the reasoning of others.
- **4.** Model with mathematics.
- **5.** Use appropriate tools strategically.
- 6. Attend to precision.
- 7. Look for and make use of structure.
- **8.** Look for and express regularity in repeated reasoning.

ESSENTIAL QUESTIONS	VOCABULARY	ASSESSMENT
 What information does the equation of a line give you? How can you make predictions based on a scatter plot? What does the slope of a line indicate about the line? What does the y-intercept indicate about a line? How do you write or identify a linear equation when given the graph of the line, two points on the line, or the slope and a point on the line? How do you represent an equation of a line using a graph, table, and equation? 	linear equation rate of change slope y-intercept x-intercept domain range origin slope-intercept form standard form point-slope form	Formative: Journals/logs KWL chart At the bell activities Question and answer Individual white boards/Promethean Board ActiVotes Homework Quizzes Constructed response/open-ended problem solving Performance tasks Exit slips Summative: CDT's Performance based assessments Quizzes Tests Constructed response/open-ended problem solving Performance based assessments Performance based assessments Project

KEYSTONE ELIGIBLE CONTENT/LEARNING PA COMMON CORE STANDARDS **ACTIVITIES** CC.2.4.8.B.1: Analyze and/or interpret bivariate data displayed in multiple representations. **A1.2.2 Coordinate Geometry** CC.2.2.8.C.2: Use concepts of functions to model relationships between quantities. CC.2.2.HS.C.1: Use the concept and notation of functions to interpret and apply them in A1.2.2.1 Describe, compute, and/or use the terms of their context. rate of change (slope) of a line. CC.2.2.HS.C.2: Graph and analyze functions and use their properties to make connections between the different representations. A1.2.2.1.1 CC.2.2.HS.C.3: Write functions or sequences that model relationships between two • Identify, describe, and/or use constant rates of change. CC.2.2.HS.C.5: Construct and compare linear, quadratic, and exponential models to solve A1.2.2.1.2 • Apply the concept of linear rate of problems. change (slope) to solve problems. **CC.2.2.HS.C.6:** Interpret functions in terms of the situations they model. CC.2.4.HS.B.1: Summarize, represent, and interpret data on a single count or measurement A1.2.2.1.3 • Write or identify a linear equation variable. CC.2.4.HS.B.2: Summarize, represent, and interpret data on two categorical and when given UNIT OF INSTRUCTION: quantitative variables. the graph of the line, CC.2.4.HS.B.3: Analyze linear models to make interpretations based on the data. two points on the line, or o the slope and a point on the **Essential Skills and Understanding** Ability to identify, describe, and/or use constant rates of change. Note: Linear equation may be in Knowledge that the rate of change of a function can be positive, negative, zero, point-slope, standard, and/or slopeintercept form. Ability to identify the rate of change from multiple representations. Ability to identify the domain and range of a function from multiple A1.2.2.1.4 Determine the slope and/or representations. y-intercept represented by a linear Ability to translate from algebraic representations to graphic or numeric equation or graph. representations and identify key features using the various representations. Ability to identify or write a linear equation when given various parts of a linear A1.2.2.2 equation, table or graph. Analyze and/or interpret data on a Ability to determine the slope and/or y-intercept represented by a linear equation scatter plot. or graph. A1.2.2.2.1 Ability to describe the restrictions on the domain of all functions based on real • Draw, identify, find, and/or write an world context. equation for a line of best fit for a Ability to focus on vertical translations of graphs of linear functions. Relate the scatter plot. vertical translation of a linear function to its y-intercept. Knowledge of the characteristics of categorical data. Ability to translate from linear algebraic representations to graphic or numeric representations and identify key features using the various representations. Ability to recognize types of relationships that lend themselves to linear models. Ability to create and use regression models to represent a contextual situation.

	DIFFERENTIATION ACTIVITIES:				
Teac	cher dir	ected differentiated instructional projects and activities are ongoing	g and k	pased o	n student need.
	•	Pearson SuccessNet On-Line Teacher's Edition		•	Pearson Success

- Pearson on-line resources and materials
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- Supporting the range of learners as per teacher manual
- Encourage and support learners in explaining how they applied their skills during mathematical tasks
- http://www.artofproblemsolving.com/liz/Alcumus/index.php
- Enrichment based on student GIEP or need of student

Pearson Successnet On-Line Teacher's Edition

- Pearson on-line resources and materials
- Web-based Math Resources
- Supporting the range of learners as per teacher manual
- Teacher generated/differentiated instruction activities
- Small group instruction
- Adapted assignments
- Additional time
- Alternative Assessments
- Chunking of content, assignment and/or assessments
- One-on-one re-teaching
- Volunteer/peer tutoring
- Accommodations based on IEP and/or need
- ELL student (or based on student need) additional support
 - o Provide specific examples
 - Use of Manipulatives
 - o Simplified language in word problems
 - Visuals
 - Flashcards
 - Multiple-meaning words
 - Bilingual dictionary/picture dictionary
- Math Support, Learning Support, or ELL Teachers as appropriate and based on need

REMEDIATION:

ENRICHMENT:

RESOURCES:

- Pearson Algebra I: Units 5, 6
- PDE SAS portal: http://www.pdesas.org
- Thinking Maps
- Graphing calculator
- Exit Tickets
- Adaptions checklist
- ELL Instructional Strategies for Math
- ESL Handbook
 - o Click on "Academic Resources" from PMSD website
 - Click on "ESL" on left side of tool bar.
 - o Click on the link to the PMSD ESEL Handbook
 - Scroll through to page 44 in the appendices.
- Teacher generated/differentiated instruction resources and activities
- Algebra I released state sample questions
- Algebra I generated sample questions
- Promethean Flipcharts/ActiveVotes
- Math flipcharts
- Math Internet Resources from PMSD Resource Page
- StudyIsland
- http://www.khanacademy.org/
- Thinkfinity website: http://www.thinkfinity.org/home
- IXL Website: http://www.IXL.com/math/
- United Streaming: http://streaming.discoveryeducation.com/index.cfm
- http://edhelper.com/place value.html
- http://illuminations.nctm.org
- http://insidemathematics.org
- www.teachingchannel.org
- www.Learnzillion.com
- http://illustrativemathematics.org/standards/k8
- http://wiki.warren.kyschools.us/groups/wcpscommoncorestandards/
- www.teachingchannel.org
- http://www.learnzillion.com
- http://www.teacherspayteachers.com
- flexmath.ck12.org/

Algebra IA: Gr. 9	MODULE 2/UNIT 6:	Linear Functions and Data Organizations: Data Analysis	TIME FRAME:	Ongoing
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NATIONAL COMMON CORE STANDARDS:

Summarize, represent, and interpret data on a single count or measurement variable.

- **S.ID.1** Represent data with plots on the real number line (dot plots, histograms, and box plots).
- **S.ID.2** Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard deviation) of two or more different data sets.
- **S.ID.3** Interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of extreme data points (outliers).

Summarize, represent, and interpret data on two categorical and quantitative variables.

- **S.ID.5** Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data.
- **S.ID.6** Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.
 - a. Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.
 - b. Informally assess the fit of a function by plotting and analyzing residuals.
 - c. Fit a linear function for a scatter plot that suggests a linear association.

Interpret linear models.

- **S.ID.7** Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data.
- **S.ID.8** Compute (using technology) and interpret the correlation coefficient of a linear fit.
- **S.ID.9** Distinguish between correlation and causation.

MATHEMATICAL PRACTICES:

- 1. Make sense of problems and persevere in solving them.
- 2. Reason abstractly and quantitatively.
- **3.** Construct viable arguments and critique the reasoning of others.
- 4. Model with mathematics.
- 5. Use appropriate tools strategically.
- **6.** Attend to precision.
- 7. Look for and make use of structure.
- **8.** Look for and express regularity in repeated reasoning.

ESSENTIAL QUESTIONS	VOCABULARY	ASSESSMENT
 How can collecting and analyzing data help you make decisions or predictions? How can you make and interpret different representations of data? How can you make predictions based on a circle, line, or bar graph; measure of central tendency; or other representation? How can you analyze data, make predications, and/or answer questions based on box-and-whisker plots, stemand-leaf plots, scatter plots, measures of central tendency, or other representations? How can you make predictions using the equations or graphs of best-fit lines for scatter plots? 	outliers quartile interquartile range measure of central tendency dependent events independent events box and whisker plots stem and leaf plots favorable outcome scatter plot line of best fit	Formative: Journals/logs KWL chart At the bell activities Question and answer Individual white boards/Promethean Board ActiVotes Homework Quizzes Constructed response/open-ended problem solving Performance tasks Exit slips Summative: CDT's Performance based assessments Quizzes Tests Constructed response/open-ended problem solving Performance based assessments Quizzes Tests Constructed response/open-ended problem solving Performance tasks Project

	PA COMMON CORE STANDARDS	KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES
	CC.2.4.HS.B.1: Summarize, represent, and interpret data on a single count or measurement variable.	A1.2.3 Data Analysis
CTION: YSIS	CC.2.4.HS.B.3: Analyze linear models to make interpretations based on the data. CC.2.4.HS.B.4: Recognize and evaluate random processes underlying statistical experiments.	A1.2.3.1 Use measures of dispersion to describe a set of data.
UNIT OF INSTRUCTION: DATA ANALYSIS	CC.2.4.HS.B.5: Make inferences and justify conclusions based on sample surveys, experiments, and observational studies.	 A1.2.3.1.1 Calculate and/or interpret the range, quartiles, and interquartile range of
NIT O	 Essential Skills and Understanding Knowledge of the characteristics of categorical data. 	data.
ī i	 Ability to read and use a two-way frequency table. Ability to read a segmented bar graph. Ability to recognize types of relationships that lend themselves to linear models. 	A1.2.3.2 Use data displays in problem-solving settings and/or to make predictions.

PA COMMON CORE STANDARDS	KEYSTONE ELIGIBLE CONTENT/LEARNING ACTIVITIES
 Ability to create and use regression models to represent a contextual situation. Ability to recognize patterns in residual plots. Ability to recognize patterns in residuals) with a calculator. Ability to recognize a linear relationship displayed in a scatter plot. Ability to determine an equation for the line of best fit for a set of data points. Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data. Knowledge of the range of values and the interpretation of those values for correlation coefficients (-1 ≤ r ≤ 1). Ability to compute and analyze the correlation coefficient for the purpose of communicating the goodness of fit of a linear model for a given data set. Ability to provide examples of two variables that have a strong correlation but one does not cause the other. 	 Estimate or calculate to make predictions based on a circle, line, bar graph, measure of central tendency, or other representation. A1.2.3.2.2 Analyze data, make predictions, and/or answer questions based on displayed data (box-and-whisker plots, stem-and-leaf plots, scatter plots, measures of central tendency, or other representations). A1.2.3.2.3 Make predictions using the equations or graphs of best-fit lines of scatter plots.

DIFFERENTIATION A	ACTIVITIES:
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Teacher directed differentiated instructional projects and activities are ongoing and based on student need.

- Pearson SuccessNet On-Line Teacher's Edition
- Pearson on-line resources and materials
- StudyIsland
- Web-based Math Resources
- Small group instruction
- Teacher generated/differentiated instruction enrichment and activities
- Supporting the range of learners as per teacher manual
- Encourage and support learners in explaining how they applied their skills during mathematical tasks
- http://www.artofproblemsolving.com/liz/Alcumus/index.php
- Enrichment based on student GIEP or need of student

- Pearson Successnet On-Line Teacher's Edition
- Pearson on-line resources and materials
- Web-based Math Resources
- Supporting the range of learners as per teacher manual
- Teacher generated/differentiated instruction activities
- Small group instruction
- Adapted assignments
- Additional time
- Alternative Assessments
- Chunking of content, assignment and/or assessments
- One-on-one re-teaching
- Volunteer/peer tutoring
- Accommodations based on IEP and/or need
- ELL student (or based on student need) additional support
 - o Provide specific examples
 - Use of Manipulatives
 - o Simplified language in word problems
 - Visuals
 - Flashcards
 - Multiple-meaning words
 - Bilingual dictionary/picture dictionary
- Math Support, Learning Support, or ELL Teachers as appropriate and based on need

REMEDIATION:

ENRICHMENT:

RESOURCES:

- Pearson Algebra I: Units 1, 6,
- PDE SAS portal: http://www.pdesas.org
- Thinking Maps
- Graphing calculator
- Exit Tickets
- Adaptions checklist
- ELL Instructional Strategies for Math
- ESL Handbook
 - o Click on "Academic Resources" from PMSD website
 - Click on "ESL" on left side of tool bar.
 - o Click on the link to the PMSD ESEL Handbook
 - Scroll through to page 44 in the appendices.
- Teacher generated/differentiated instruction resources and activities
- Algebra I released state sample questions
- Algebra I generated sample guestions
- Promethean Flipcharts/ActiveVotes
- Math flipcharts
- Math Internet Resources from PMSD Resource Page
- StudyIsland
- http://www.khanacademy.org/
- Thinkfinity website: http://www.thinkfinity.org/home
- IXL Website: http://www.IXL.com/math/
- United Streaming: http://streaming.discoveryeducation.com/index.cfm
- http://edhelper.com/place_value.html
- http://illuminations.nctm.org
- http://insidemathematics.org
- www.teachingchannel.org
- www.Learnzillion.com
- http://illustrativemathematics.org/standards/k8
- http://wiki.warren.kyschools.us/groups/wcpscommoncorestandards/
- www.teachingchannel.org
- http://www.learnzillion.com
- http://www.teacherspayteachers.com
- <u>flexmath.ck12.org/</u>